# Introduction to Jax from the lens of computational biology

**CCB Skills Seminar** Martin Kim (Yosef Lab, UC Berkeley)

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#### **CCB** CENTER FUR COMPUTATIONAL BIOLOGY



## Link for following along

#### Colab notebook: <u>https://tinyurl.com/ccb-intro-to-jax</u>

### Plan for today

#### What is Jax? Overview of its main features

#### Exploring its main features with an extended example

#### Why use Jax? Its ecosystem and some projects

Open-source machine learning library in Python developed by Google

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- Interface inspired by NumPy
- Emphasis on functional programming



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#### numpy.ndarray

#### jax.numpy.ndarray

#### JAX



Compiles user-written code using various optimizations

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#### JAX



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Computes gradients through Jax and native Python code

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from jax import grad

Provide efficient kernels and automatic vectorization

from jax import **vmap** 

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**K-means clustering** 

Cluster assignments for each cell

**Just-in-time compilation:** Jax can complete Python program and cache functions

Python program and cache functions

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How it works: Jax drops an abstract array into the function and traces how it is affected in order to optimize the function

### JIT compilation: demo

Logistic regression cost function

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- e.g. forward pass or a gradient update to the parameters in an neural net

## **Example: PCA**

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- 2. principal coordinates  $\leftarrow \sigma \odot U$ , diag $(\sigma) = \Sigma$
- 3. take first *n* principal coordinates

## JIT compilation: demo

Principal components analysis

code to device-specific kernels (CPU, GPU, TPU)

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result = vmap\_my\_func(X)

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### XLA & vectorization: demo

Pairwise Euclidean distances

### **Example: k-means clustering**

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**Expectation step:**  $y_i \leftarrow \arg \min \| \mathbf{x} \|$ 

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### **Example: k-means clustering** Goal: Cluster our data using k-means for visualization and labeling Given data $X \in \mathbb{R}^{N \times D}$ and fixed number of clusters k: Find $\mu_i$ that minimize $\sum_{i=1}^{k} \sum_{j=1}^{k} \|\mathbf{x}_j - \mu_i\|_2^2$ $i=1 \mathbf{x}_i \in S_i$ 2 **Expectation step:** $y_i \leftarrow \arg \min \| \mathbf{x} \|$ Maximization step: $\mu_i \leftarrow \frac{1}{|S_i|} \sum_{i \in S_i} \sum_{$ $\mathbf{X}_i \in S_i$

$$\mathbf{x}_j - \boldsymbol{\mu}_i \|_2^2$$
  
 $\mathbf{x}_j$ 

### XLA & vectorization: demo

K-means clustering with Lloyd's method

## Autograd

Jax provides automatic differentiation as part of its core functionality:

grad\_my\_func = jax.grad(my\_func)

derivative = grad\_my\_func(1.5)

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value and then applies derivative rules.

- Similar to JIT compilation, Jax **traces** the operations that affect a particular

### Autograd: demo

Plotting simple functions and their derivatives

Goal: Use Newton's method to optimizer our loss function

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**Maximization step**:  $\mu_i \leftarrow \mu_i - \mathbb{H}^{-1} \frac{\partial \mathscr{L}}{\partial \Omega}$ 

 $\begin{aligned} & -\mu_i \|_2^2 \\ & \partial \mathscr{L} \\ & \partial \mu_i \end{aligned}$ 



### Autograd: demo

### K-means clustering with Newton's method



Binary cross-entropy loss for logistic regression

Principal component analysis

### JAX



Binary cross-entropy loss for logistic regression

**Principal component analysis** 



Pairwise Euclidean distances between vectors

**K-means clustering** 



Binary cross-entropy loss for logistic regression

**Principal component analysis** 

Derivatives of polynomials and piecewise functions

Newton's method

Pairwise Euclidean distances between vectors

**K-means clustering** 

### Other topics not covered here

- jax.scipy: SciPy API
- jax.pmap: parallel execution on multiple devices
- jax.lax: lower-level functions for more custom operations
- **PyTrees:** an essential data structure in Jax
- Random number generation
- Ahead-of-time compilation
- Forward- and reverse-mode autodiff



## Why use Jax? Its ecosystem

- Flax: Neural network library
- **Optax:** Gradient processing and optimizers
- Jraph: Graph neural networks
- NumPyro: Probabilistic programming
- HuggingFace: Pretrained models

### JAX, M.D.

A Framework for Differentiable Physics

Samuel S. Schoenholz Google Research: Brain Team schsam@google.com Ekin D. Cubuk Google Research: Brain Team cubuk@google.com

### **Molecular dynamics**

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**Structure prediction** 

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JOURNAL ARTICLE

### End-to-end learning of multiple sequence alignments with differentiable Smith–Waterman a

Samantha Petti, Nicholas Bhattacharya, Roshan Rao, Justas Dauparas, Neil Thomas, Juannan Zhou, Alexander M Rush, Peter Koo, Sergey Ovchinnikov 💌

Bioinformatics, Volume 39, Issue 1, January 2023, btac724, https://doi.org/10.1093 /bioinformatics/btac724 Published: 10 November 2022 Article history ▼ Differentiable multiple sequence alignment

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### End-to-end learning of multiple sequence alignments with differentiable Smith–Waterman 👌

### **Differentiable multiple** sequence alignment

### scib-metrics

build passing docs passing

### **Biological metrics** and benchmarks

Accelerated and Python-only metrics for benchmarking single-cell integration outputs.

This package contains implementations of metrics for evaluating the performance of single-cell omics data integration methods. The implementations of these metrics use jax when possible for jitcompilation and hardware acceleration. All implementations are in Python.
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#### Large language models

## Thanks for listening! Questions?

Colab notebook: https://tinyurl.com/ccb-intro-to-jax

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